

Sorrento

SAPEM' 23

常熟

Acoustic Modeling of Granular Material and its Combination with a Flexible Perforated Membrane



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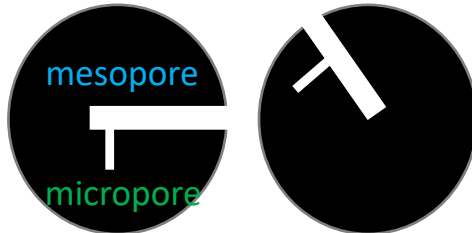
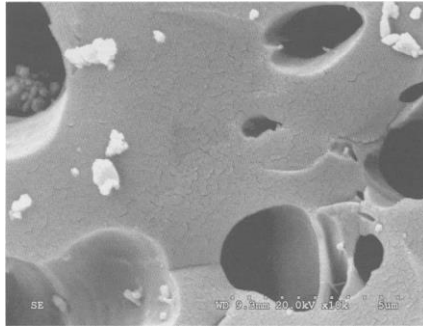
PART 01

Introduction

Hierarchical Porous Particles



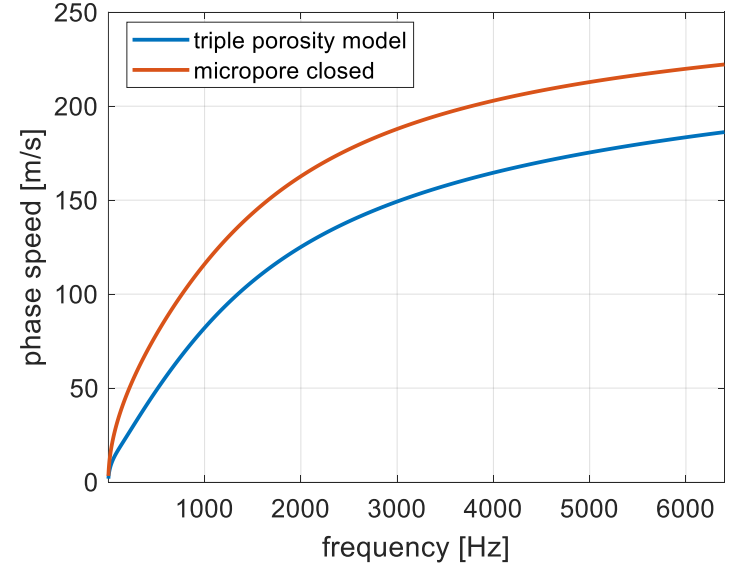
- SEM image of activated carbon (Marsh and Rodríguez-Reinoso, *Activated Carbon*, 2006)



interstitial pores

Triple porosity model for granular activated carbon (GAC)
(Venegas and Umnova, 2016)

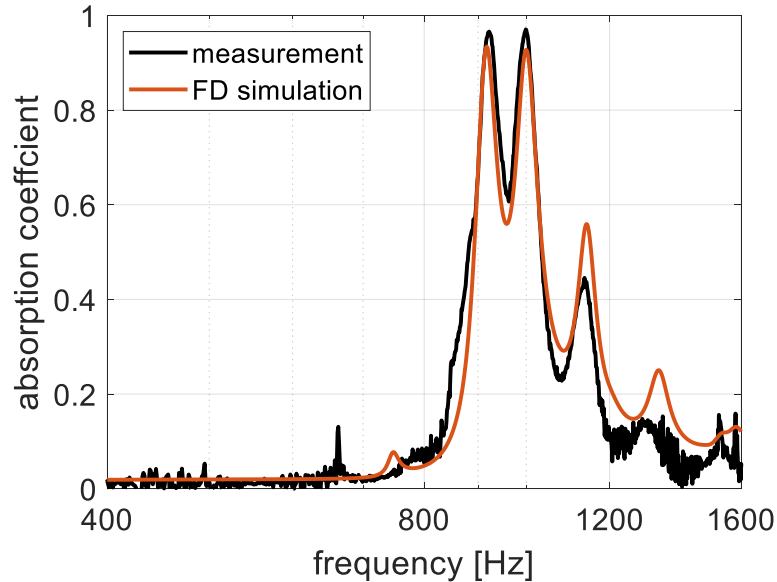
- The micropores inside the granules can **lower the speed of sound** in the material, provides larger apparent volume:



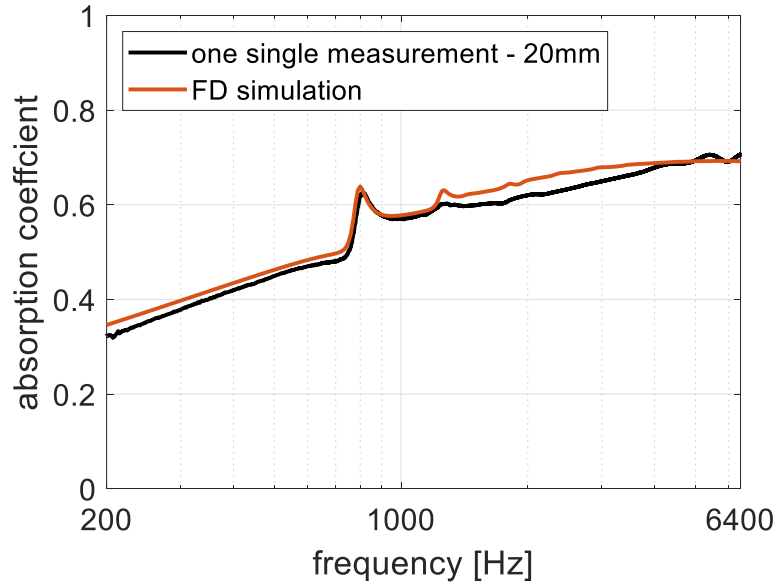
Particle 2-D Finite Difference Modeling



- In our previous study, with the 2-D Finite Difference method, acoustics response of different particles in impedance tube was successfully reconstructed



20-mm-thick glass bubble

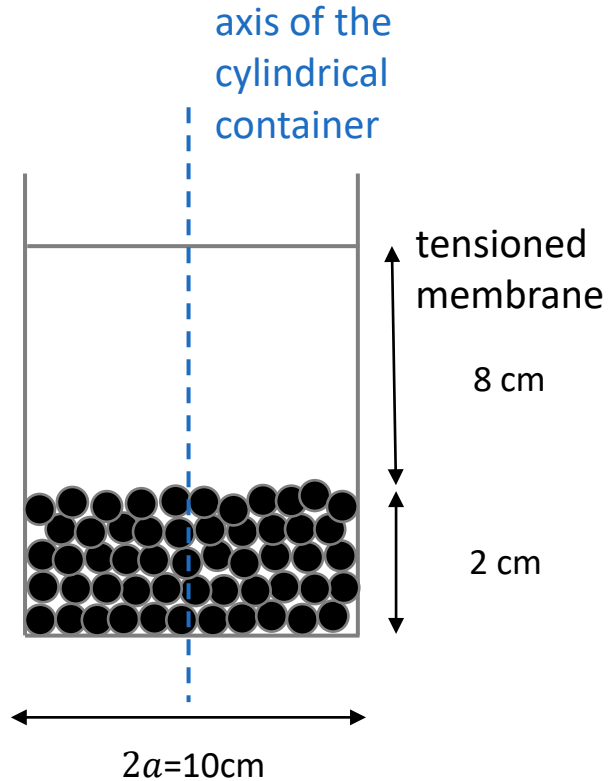


20-mm-thick GAC

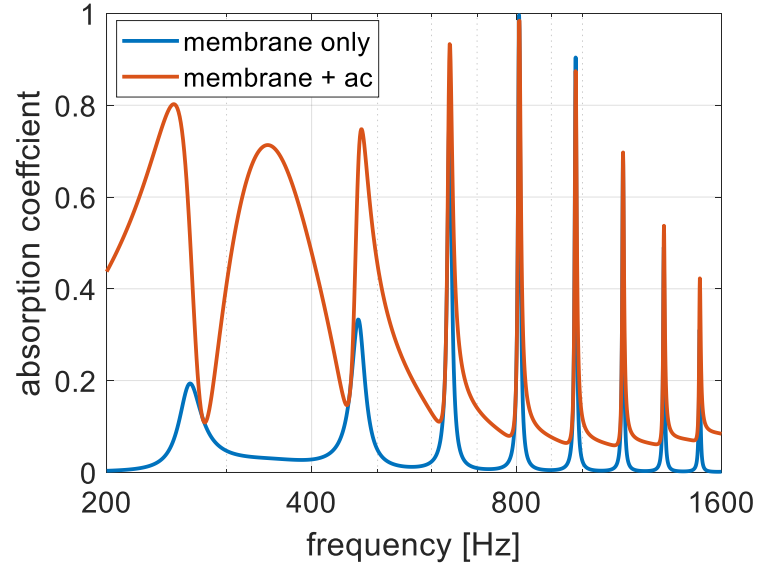
GAC Infilled Membrane Sound Absorber



A set of parameters was chosen so that the surface impedance predicted by the triple porosity model matches closely to that reported in (Arenas et al., 2023):



- GAC helps improve the low frequency performance.



Model predictions that closely match those in figure 2(a) and 3(b) from Arenas et al., 2023.

PART 02

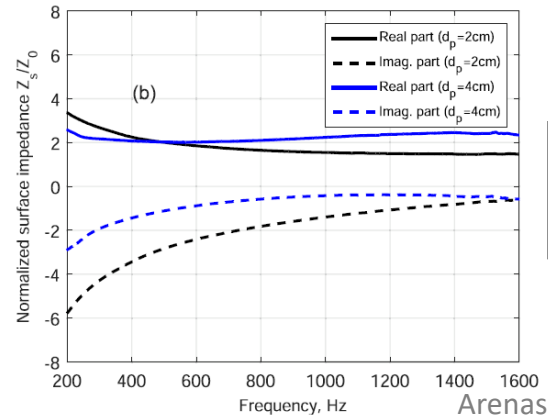
Modeling Method

Porous Granules

- A recent study (Arenas et al., 2023) looked into the performance of an absorber consisting of GAC and a membrane using a 1D model

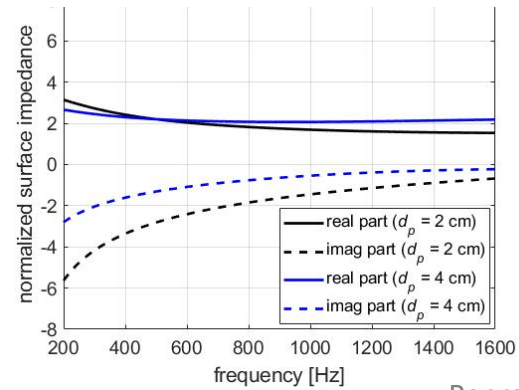
r_p [mm]	granule radius	0.29
r_m [μm]	mesopore radius	0.1973
r_n [nm]	micropore radius	1
ϕ_p	macroporosity	0.4059
ϕ_m	mesoporosity	0.3878
ϕ_n	microporosity	0.4285
b [Pa^{-1}]	Langmuir constant	4.919×10^{-7}
D_c [m^2/s]	configurational diffusivity	5×10^{-9}

Total porosity: 0.7922
 Bulk density: 457 kg/m³



2 or 4 cm

Arenas et al., 2023



Porous Granules

Further, the stiffness of the “frame” consisting of the unconsolidated granules was accounted for by applying Biot theory (poroelastic model).

The governing equations can be found in (Biot, 1956):

$$N\nabla^2 \mathbf{u} + \nabla[(A + N)e + Q\varepsilon] = \frac{\partial^2}{\partial t^2} (\rho_{11} \mathbf{u} + \rho_{12} \mathbf{U})$$

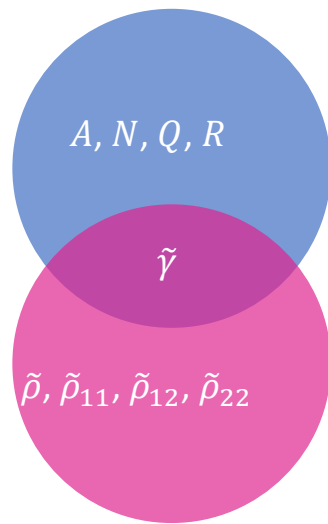
$$\nabla(Qe + R\varepsilon) = \frac{\partial^2}{\partial t^2} (\rho_{12} \mathbf{u} + \rho_{22} \mathbf{U})$$

For the purpose of implementing the FD scheme, the $\mathbf{u} - p$ formulation (Atalla et al., 1998) is applied:

$$\nabla \cdot \hat{\sigma}^s + \omega^2 \tilde{\rho} \mathbf{u} + \tilde{\gamma} \nabla p = 0$$

$$\nabla^2 p + \omega^2 \frac{\tilde{\rho}_{22}}{R} p - \omega^2 \frac{\tilde{\rho}_{22}}{\phi^2} \tilde{\gamma} \nabla \cdot \mathbf{u} = 0$$

Stiffness coefficients



K_{eq}, ρ_{eq}

Density coefficients

Membranes

- Tensioned Membrane (Arenas et al., 2023):

$$T\nabla^2 w + \Delta p = \rho_s \frac{\partial^2 w}{\partial t^2}$$

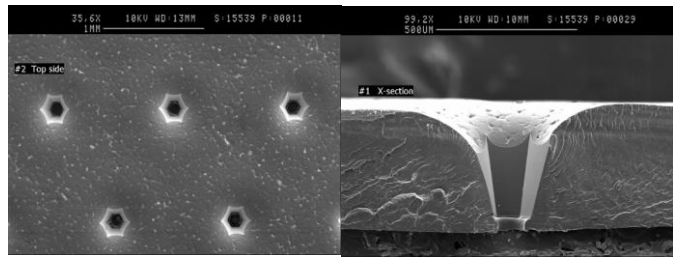
Spatial average
1D impedance



$$Z_m = j\omega\rho_s \left[1 - \frac{2}{k_m a} \frac{J_1(k_m a)}{J_0(k_m a)} \right]^{-1}$$

$$k_m = \omega\sqrt{\rho_s/T}$$

- Micro-Perforated Membrane (Yoo et al., 2008)



$$\Delta p - R_t \Omega \frac{\partial(d_f - d_s)}{\partial t} = \rho_f h \frac{\partial^2 d_f}{\partial t^2}$$

$$\Delta p + R_t \frac{\Omega}{1 - \Omega} \frac{\partial(d_f - d_s)}{\partial t} = D\nabla^4 d_s - T\nabla^2 d_s + \rho_s \frac{\partial^2 d_s}{\partial t^2}$$

Flexural stiffness

Tension

Surface density

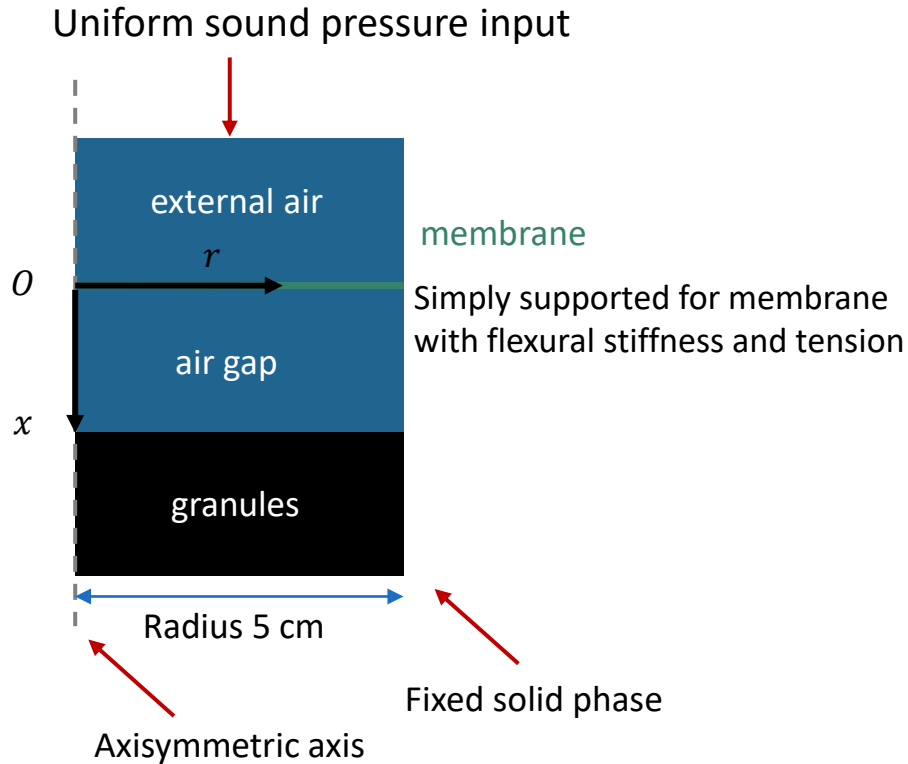
Front side and cross-section of a micro-perforated membrane (Yoo et al., 2008)

(Maa, 1998):

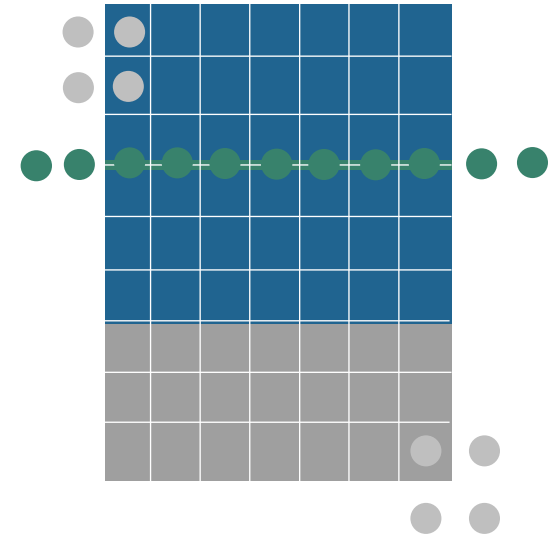
$$Z = j\omega\rho_0 h \left[1 - \frac{2}{g\sqrt{-j}} \frac{J_1(g\sqrt{-j})}{J_0(g\sqrt{-j})} \right]^{-1}, g = r \sqrt{\frac{\rho_0 \omega}{\eta}}$$

The displacement of a perforated membrane can be described as follows (Yoo et al., 2008): $w = \Omega d_f + (1 - \Omega)d_s$

2-D Finite Difference Simulation



2D five point stencil

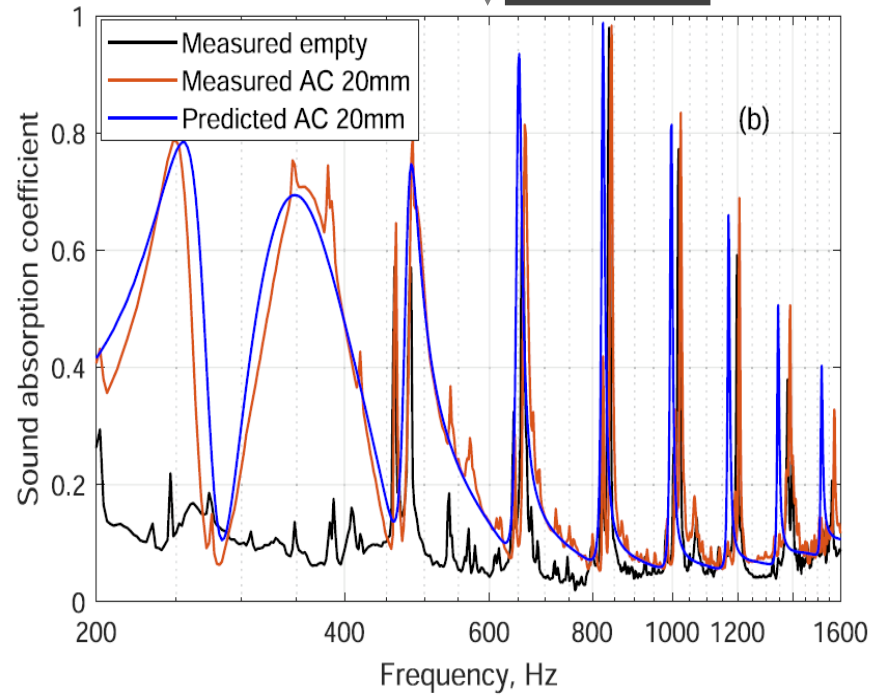
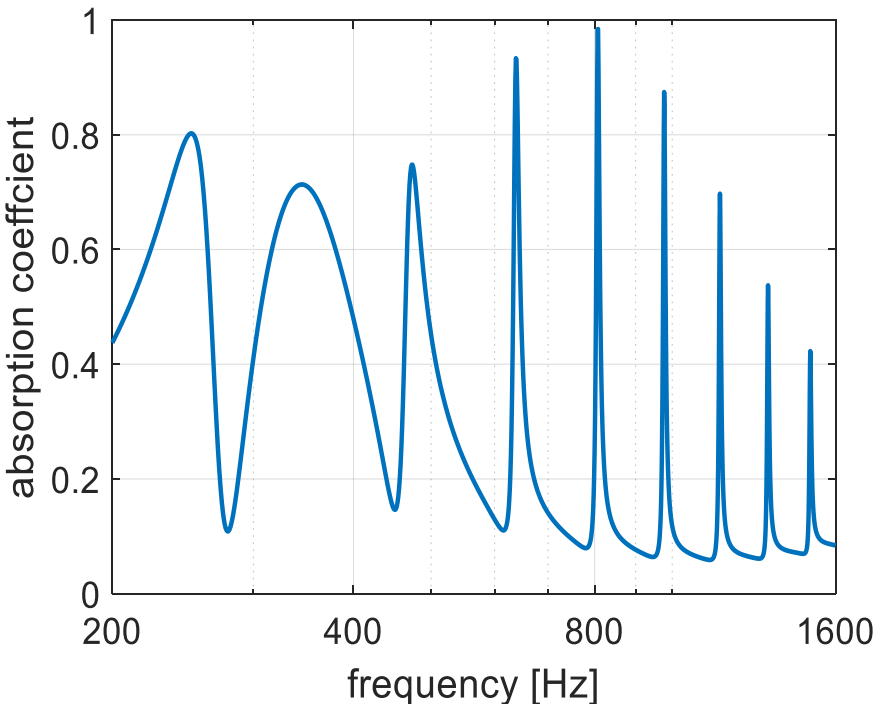
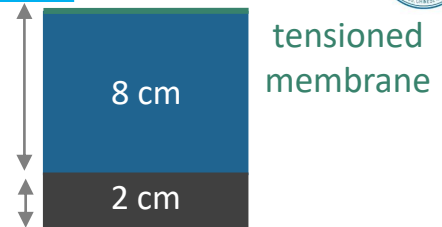


PART 03

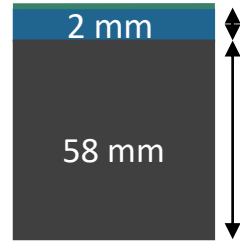
Simulation Result

Membrane + Particle 1-D Simulation

- **Good match between measurements and 1D predictions with large air gap**



2-D Simulation Study

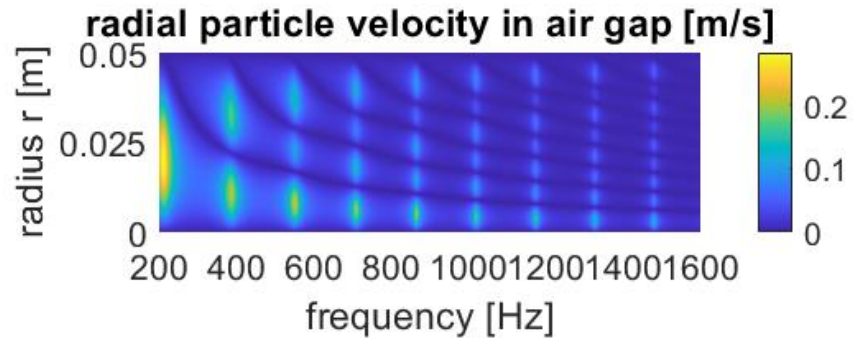
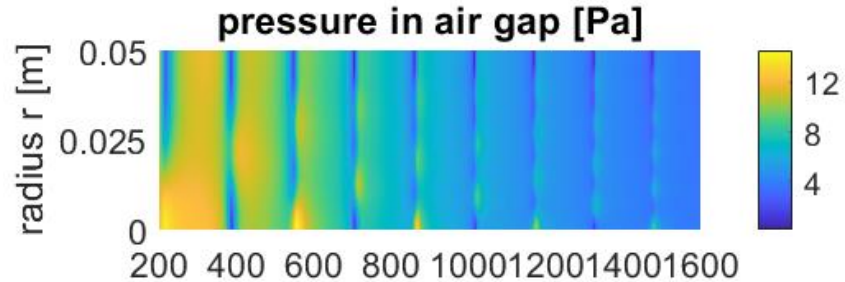
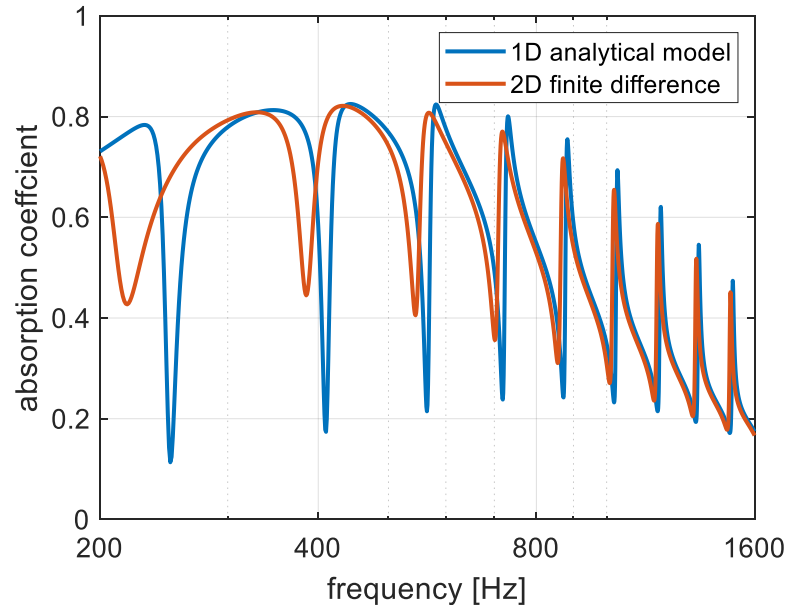


Tensioned membrane:

$$\rho_s = 0.265 \text{ kg/m}^3$$

$$T = 62 \times (1 + 0.005j) \text{ N/m}$$

58 mm GAC + 2 mm air gap



- It is necessary to consider the radial modes
- Radial fluid motion in granule stack dissipates energy: i.e., “Nearfield damping”

2-D Simulation Study

Tensioned membrane:

$$\rho_s = 0.265 \text{ kg/m}^3$$

$$T = 55.2 \times (1 + 0.005j) \text{ N/m}$$

18 mm GAC + 2 mm air gap

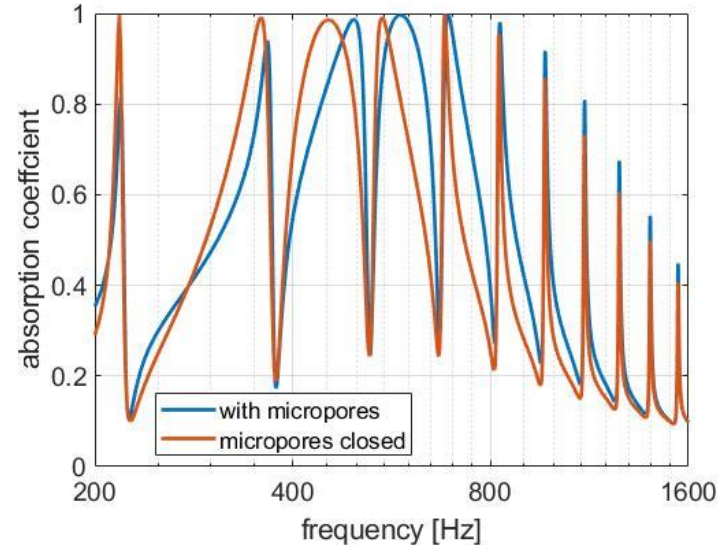
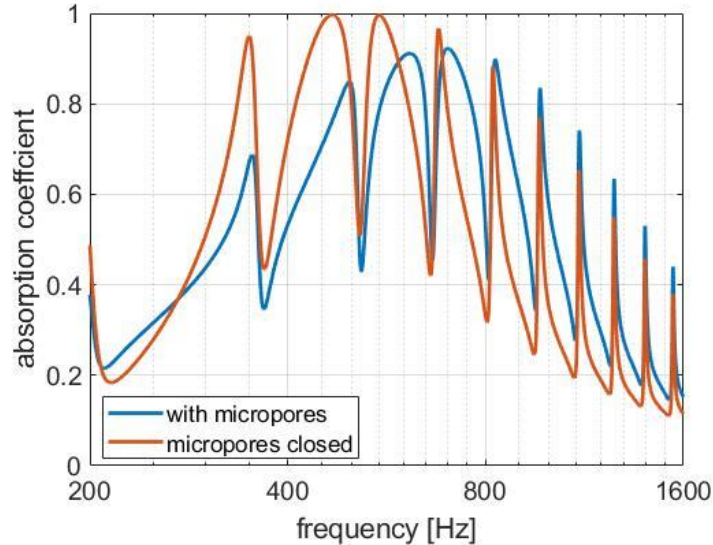
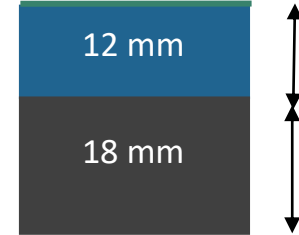


Tensioned membrane:

$$\rho_s = 0.265 \text{ kg/m}^3$$

$$T = 55.2 \times (1 + 0.005j) \text{ N/m}$$

18 mm GAC + 12 mm air gap



- **More significant impact of GAC pores with narrow gap**

2-D Simulation Study



Perforated membrane: tension + flexural stiffness + finite flow resistance

$$\rho_s = 0.912 \text{ kg/m}^3$$

$$h = 0.8 \text{ mm}$$

$$T = 50.04 \times (1 + 0.005j) \text{ N/m}$$

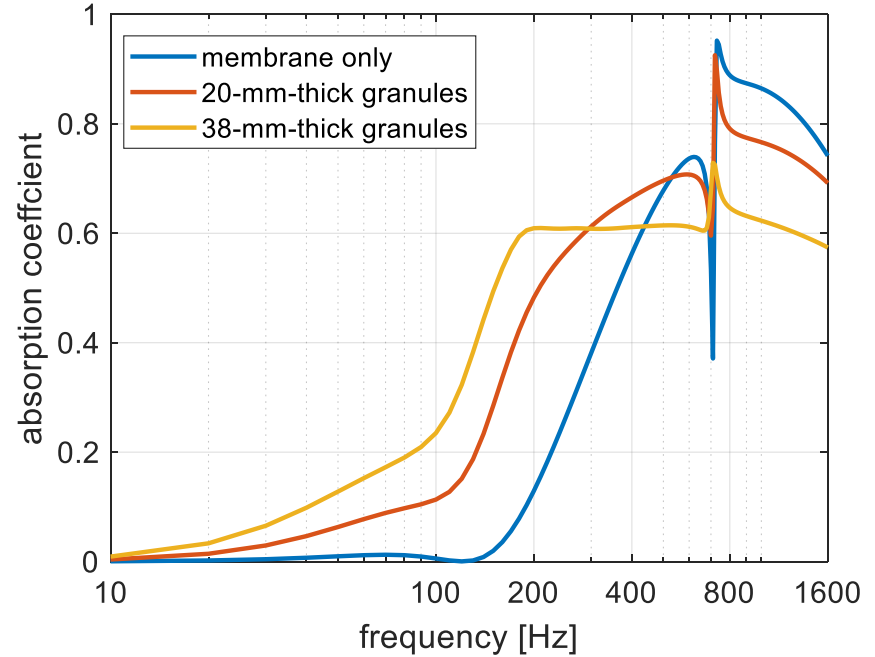
$$\Omega = 0.02$$

$$r = 0.15 \text{ mm}$$

$$D = 0.1313 + 0.0007j \text{ Pa} \cdot \text{m}^3$$

$$R_{t0} = 1.03 \times 10^3 \text{ rayl}$$

Total cavity depth: 40 mm



- **GAC contributes to higher low frequency absorption**
- **The simulation of narrow gap predicts obvious increase at low frequency**

PART 04

Conclusion

Conclusion



A 2DFD model was built to simulate the performance of absorbers consisting of membrane and porous granules:

- 1. The comparison between the 2DFD simulation and 1D analytical model prediction shows that it is necessary to consider the modal response in the radial direction when separation between membrane and granules is small**
- 2. The simulation shows potential advantages of bringing the granules close to the membrane, where the interaction of the membrane nearfield and the granule stack may be exploited to increase energy dissipation and to reduce reflection**
- 3. The simulation of the absorber with a perforated membrane shows more dramatic improvement at low frequencies when GAC is added to the absorber**

In the future, it is of interest to experimentally validate the predictions of the 2DFD model, and find theoretical explanation of the difference with the 1D model prediction, especially when the air gap is narrow

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Thanks for your attention!